

# High School Exit Examination

## Mathematics

### Overhead Masters\*

- Content standards to be covered
- Use of calculators; formulas provided
- Sample test items
- Standards being assessed



**Updated December 15, 2000**

*\* Taken from HSEE in Mathematics Teacher Guide: Part I*

# **Mathematics Revisions**

- Revisions made in Overhead Masters since the November 14, 2000 edition in this document:

**Pages:**

- 2 – total number of test items updated
- 40 thru 45 – (sample items) removed



# HSEE Mathematics

◆ Content standards to be covered:	Total Items
● Grade 6–Statistics, Data Analysis, and Probability	6
● Grade 7–Number Sense	14
● Grade 7–Algebra and Functions	17
● Grade 7–Measurement and Geometry	17
● Grade 7–Statistics, Data Analysis and Probability	6
● Grade 7–Mathematical Reasoning	8
● Algebra I	12

*Mathematics Teacher Guide: Part I — Pages 18–29*

# For the HSEE in Mathematics

- ◆ Calculators cannot be used
- ◆ Formulas will not be provided for the most common conversions but will be included for conversions between systems

# Statistics, Data Analysis, and Probability (Grade 6)

**3.3** Represent probabilities as ratios, proportions, decimals between 0 and 1, and percentages between 0 and 100 and verify that the probabilities computed are reasonable; know that if  $P$  is the probability of an event,  $1-P$  is the probability of an event not occurring.



# Sample Mathematics Item

*Statistics, Data Analysis, and Probability (Grade 6)—3.3*

- ◆ Rosella is rolling a numbered cube with the numbers 1 through 6 on it. She rolls the cube twice. What is the probability the two rolls will have a sum of 10?

A  $\frac{1}{36}$

B  $\frac{1}{12}$

C  $\frac{1}{10}$

D  $\frac{1}{9}$

*Mathematics Teacher Guide: Part I — Page 7*

# Statistics, Data Analysis, and Probability (Grade 7)

- 1.3** Understand the meaning of, and be able to compute the minimum, the lower quartile, the median, the upper quartile, and the maximum of a data set.



# Sample Mathematics Item

*Statistics, Data Analysis, and Probability (Grade 7)—1.3*

- ◆ Twenty students took a math test. The upper quartile value of the test scores is the median of the
  - A top four scores.
  - B top five scores.
  - C top ten scores.
  - D middle five scores.

*Mathematics Teacher Guide: Part I — Page 8*





# Number Sense

## **1.3** Convert fractions to decimals and percents and use these representations in estimations, computations, and applications.



# Sample Mathematics Item

Number Sense—1.3

- ◆ At a recent school play, 504 of the 840 seats were filled. What percent of the seats were empty?
- A      33.6%
- B      40%
- C      50.4%
- D      60%

Mathematics Teacher Guide: Part I — Page 8



# Number Sense

**1.6** Calculate the percentage of increases and decreases of a quantity.



# Sample Mathematics Item

Number Sense—1.6

- ◆ Between 6:00 A.M. and noon, the temperature went from  $45^{\circ}$  to  $90^{\circ}$ . By what percentage did the temperature increase between 6:00 A.M. and noon?
- A 45%
- B 50%
- C 55%
- D 100%

Mathematics Teacher Guide: Part I — Page 8



# Number Sense

- 1.7** Solve problems that involve discounts, markups, commissions, and profit and compute simple and compound interest.



# Sample Mathematics Item

Number Sense—1.7

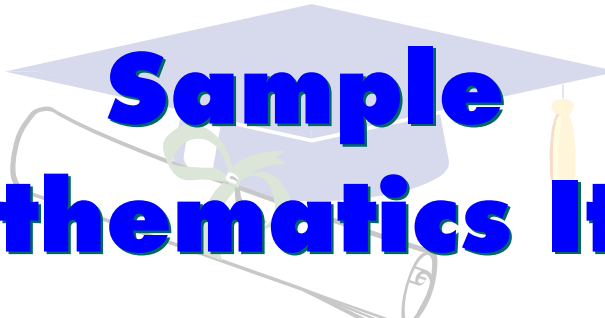
- ◆ Mr. Yee invested \$2,000 in a savings account that pays an annual interest rate of 4% compounded twice a year. If Mr. Yee does not deposit or withdraw any money, how much will he have in the bank after one year?
- A     \$2,080.00
- B     \$2,080.80
- C     \$2,160.00
- D     \$2,163.20

Mathematics Teacher Guide: Part I — Page 9



# Number Sense

- 2.1** Understand negative whole-number exponents. Multiply and divide expressions involving exponents with a common base.



# Sample Mathematics Item

Number Sense—2.1

◆  $3^2 \cdot 3^{-3}$

A  $-3$

B  $\frac{1}{3^6}$

C  $\frac{1}{3}$

D  $3$

Mathematics Teacher Guide: Part I — Page 9





# Number Sense

## **2.2** Add and subtract fractions by using factoring to find common denominators.



# Sample Mathematics Item

Number Sense—2.2

- ◆ Which of the following can be used

to compute  $\frac{3}{4} + \frac{5}{6}$ ?

A  $\frac{3+5}{4+6}$

B  $\frac{3 \cdot 3}{4 \cdot 3} + \frac{5 \cdot 2}{6 \cdot 2}$

C  $\frac{3}{4 \cdot 3} + \frac{5}{6 \cdot 2}$

D  $\frac{3}{4 \cdot 6} + \frac{5}{4 \cdot 6}$

Mathematics Teacher Guide: Part I — Page 10



# Algebra and Functions

**2.1** Interpret positive whole-number powers as repeated multiplication and negative whole-number powers as repeated division or multiplication by the multiplicative inverse. Simplify and evaluate expressions that include exponents.



# Sample Mathematics Item

Algebra and Functions—2.1

- ◆ Simplify the expression shown below

$$2x^{-3}$$

A  $\frac{8}{x^3}$

B  $(2x)^{-1}(2x)^{-1}(2x)^{-1}$

C  $\frac{2}{x^3}$

D  $\frac{1}{(2x)^3}$

Mathematics Teacher Guide: Part I — Page 10



# Algebra and Functions

**4.1** Solve two-step linear equations and inequalities in one variable over the rational numbers, interpret the solutions in the context from which they arose, and verify the reasonableness of the results.



# Sample Mathematics Item

*Algebra and Functions—4.1*

- ◆ Before each game, the Harbor High Mudcats sell programs for \$1.00 per program. To print the programs, the printer charges \$60 plus \$0.20 per program. How many programs does the team have to sell to make a profit of \$200?
  - A 250 programs
  - B 300 programs
  - C 325 programs
  - D 350 programs

*Mathematics Teacher Guide: Part I — Page 11*



# Algebra and Functions

**4.2** Solve multistep problems involving rate, average speed, distance, and time or a direct variation.



# Sample Mathematics Item

*Algebra and Functions—4.2*

- ◆ A person drove for 6 hours at an average speed of 45 miles per hour (mph) and for 9 hours at an average speed of 55 mph. Find the average speed for the entire trip.
- A 50 mph
  - B 51 mph
  - C 52 mph
  - D 53 mph

*Mathematics Teacher Guide: Part I — Page 11*





# Measurement and Geometry

- 1.1** Compare weights, capacities, geometric measures, times, and temperatures within and between measurement systems (e.g., miles per hour and feet per second, cubic inches to cubic centimeters).



# Sample Mathematics Item

Measurement and Geometry—1.1

- ◆ Order the following three speeds from fastest to slowest: 3,100 yd/hr, 160 ft/min, 9,200 ft/hr

- |   |             |             |             |
|---|-------------|-------------|-------------|
| A | 9,200 ft/hr | 3,100 yd/hr | 160 ft/min  |
| B | 9,200 ft/hr | 160 ft/min  | 3,100 yd/hr |
| C | 160 ft/min  | 9,200 ft/hr | 3,100 yd/hr |
| D | 160 ft/min  | 3,100 yd/hr | 9,200 ft/hr |

Mathematics Teacher Guide: Part I — Page 12

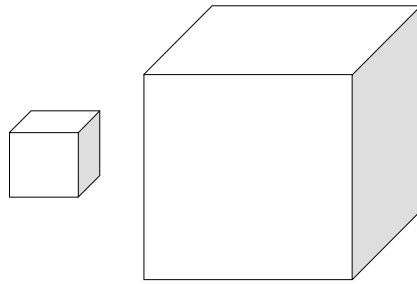


# Measurement and Geometry

- 2.3** Compute the length of the perimeter, the surface area of the faces, and the volume of a three-dimensional object built from rectangular solids. Understand that when the lengths of all dimensions are multiplied by a scale factor, the surface area is multiplied by the square of the scale factor and the volume is multiplied by the cube of the scale factor.

# Sample Mathematics Item

Measurement and Geometry—2.3



- ◆ In the figure above, an edge of the larger cube is 3 times the edge of the smaller cube. What is the ratio of the surface area of the smaller cube to that of the larger cube?
- A      1:3
- B      1:9
- C      1:12
- D      1:27

Mathematics Teacher Guide: Part I — Page 12

# Measurement and Geometry

**2.4** Relate the changes in measurement with a change of scale to the units used (e.g., square inches, cubic feet) and to conversions between units (1 square foot = 144 square inches or  $[1\text{ft}^2] = [144\text{in}^2]$ , 1 cubic inch is approximately 16.38 cubic centimeters or  $[1\text{in}^3] = [16.38\text{cm}^3]$ ).



# Sample Mathematics Item

Measurement and Geometry—2.4

◆ How many square feet are in 5 square yards?

A 15

B 25

C 45

D 60

Mathematics Teacher Guide: Part I — Page 13



# Mathematical Reasoning

## **2.4** Make and test conjectures by using both inductive and deductive reasoning.



# Sample Mathematics Item

## *Mathematical Reasoning—2.4*

- ◆ While preparing for the local marathon, Angela made the following statements:

If I do not stretch before the race, I will get muscle cramps.

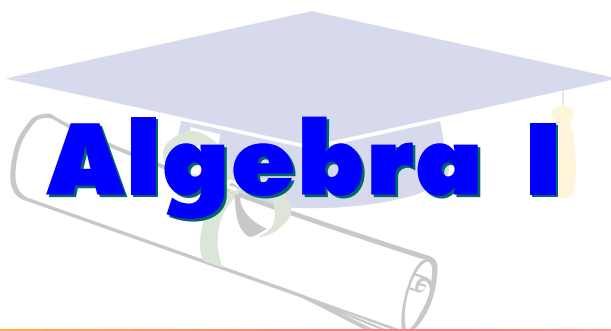
If I get muscle cramps, it will be too painful to run.

If it is too painful to run, I will not finish the race.

Based on Angela's statements, what can be concluded?

- A If she finishes the race, Angela stretched before the race.
- B If she did not finish the race, Angela had painful muscle cramps.
- C If she stretches before the race, Angela will finish the race.
- D If she has muscle cramps, Angela did not stretch before the race.





### **3.0** Students solve equations and inequalities involving absolute values.



# Sample Mathematics Item

Algebra I–3.0

- ◆ Assume  $k$  is an integer and solve for  $k$ .

$$10 - 2|k| > 4$$

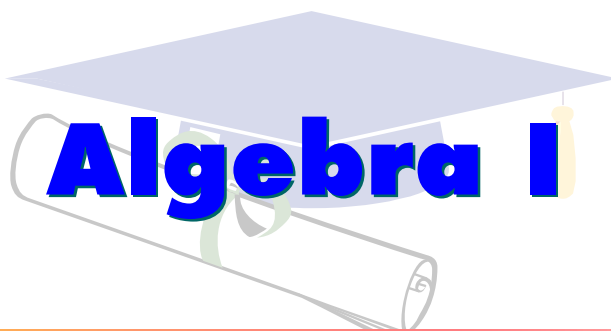
A  $\{-3, -2, -1, 1, 2, 3\}$

B  $\{-3, -2, -1, 0, 1, 2\}$

C  $\{-2, -1, 0, 1, 2\}$

D  $\{-2, -1, 1, 2, 3\}$

Mathematics Teacher Guide: Part I — Page 14



**4.0** Students simplify expressions before solving linear equations and inequalities and in one variable, such as

$$3(2x - 5) + 4(x - 2) = 12.$$



# Sample Mathematics Item

Algebra I–4.0

◆ Which of the following is equivalent to  $3x - (2 - x) < 2x - 5$ ?

A  $3x - 2 - x < 2x - 5$

B  $4x + 2 < 2x - 5$

C  $4x - 2 < 2x - 5$

D  $6x + x < 2x - 5$

Mathematics Teacher Guide: Part I — Page 14



# Algebra I

**7.0** Students verify that a point lies on a line, given an equation of the line. Students are able to derive linear equations.



# Sample Mathematics Item

Algebra I–7.0

- ◆ What is the equation of the line that includes the point  $(9, 3)$  and has a slope of  $-\frac{4}{3}$ ?

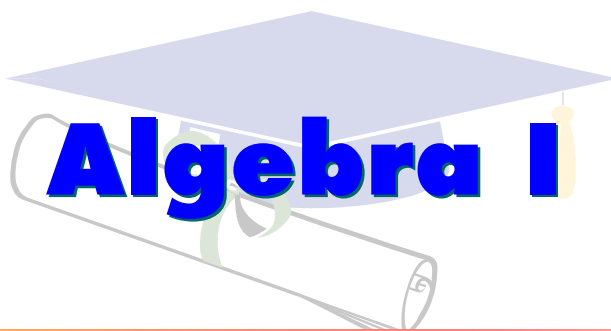
A  $y = 3x - \frac{4}{3}$

B  $y = -\frac{4}{3}x + 13$

C  $y = -\frac{4}{3}x + 15$

D  $y = \frac{1}{3}x - \frac{4}{3}$

Mathematics Teacher Guide: Part I — Page 15



**10.0** Students add, subtract, multiply, and divide monomials and polynomials. Students solve multistep problems, including word problems, by using these techniques.

# Sample Mathematics Item

Algebra I–10.0

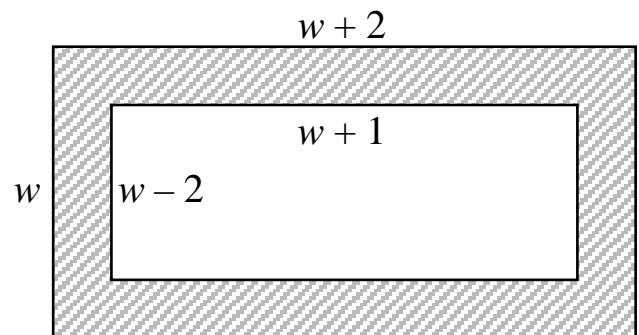
- ◆ The two rectangles below have dimensions as shown. Which of the following expressions represents the area of the shaded region?

A  $3w + 2$

B  $3w - 2$

C  $w + 2$

D  $w - 2$



Mathematics Teacher Guide: Part I — Page 15